

Electrostatic Energy and Potential

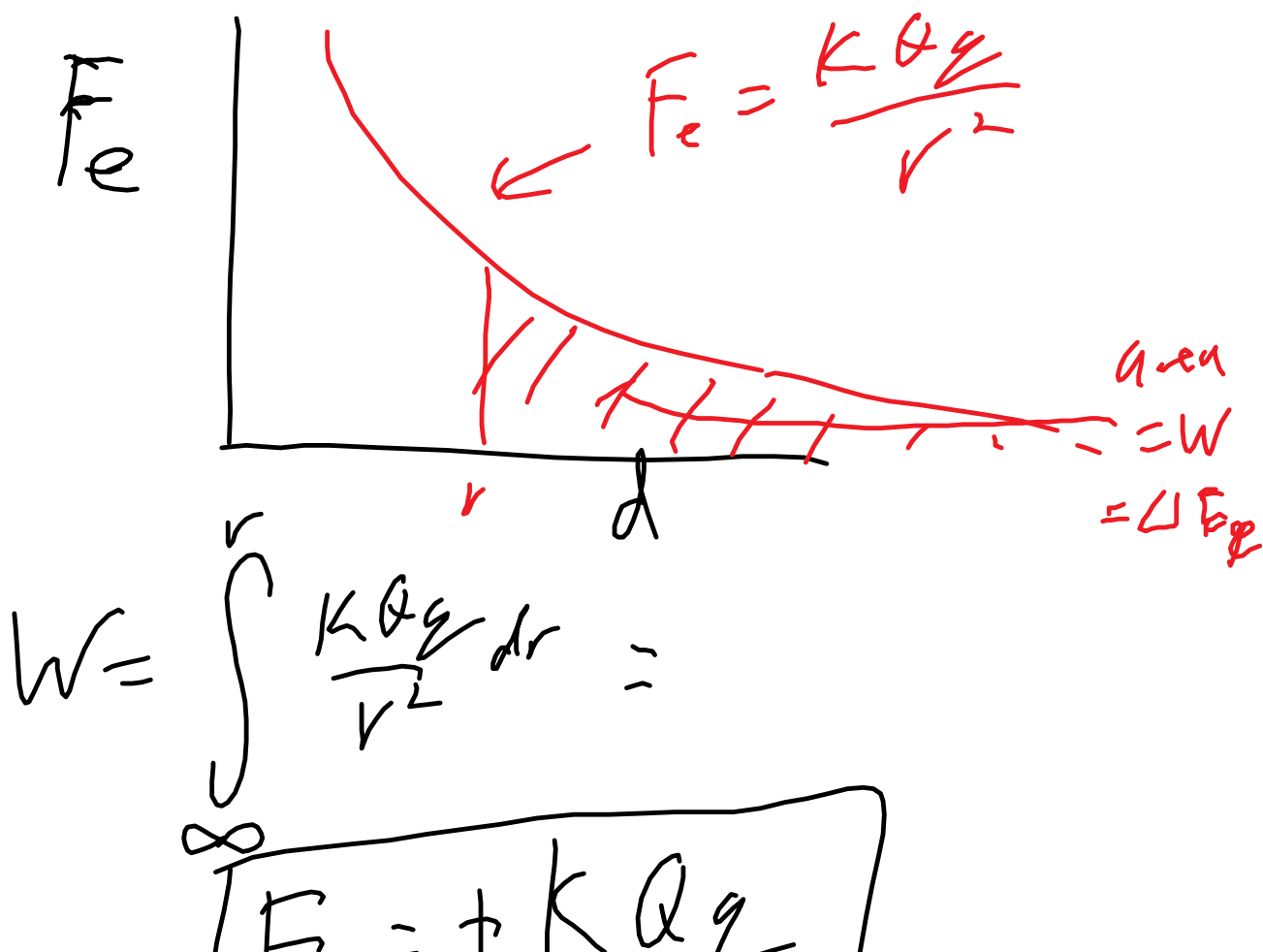
Electrostatic energy, E_e (don't confuse it with E electric field strength, F_e/q)

Derive equations using work-energy theorem

$$W_e = \Delta E_e$$

Work required to move a charge q to that point.

For two point charges, Q and q , the electrostatic energy is the work done moving q from infinity to a position, r , away from the centre of Q .

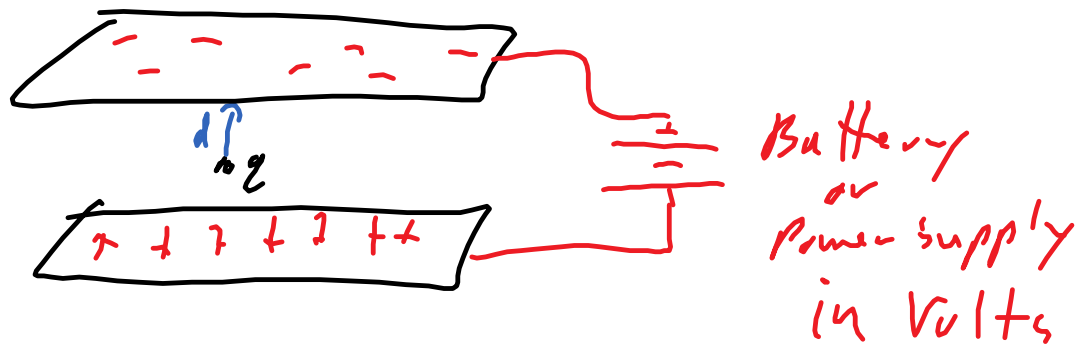


$$E_e = + \frac{K Q q}{r}$$

$$W = K Q q \left(\frac{1}{r_f} - \frac{1}{r_i} \right) = \Delta E_e$$

for Set uniform field $E = \frac{F}{q}$

$$W = Fd = Eqd = \Delta E_e$$



What is Voltage? (also called Potential)
Electrical energy per unit charge.

$$V = E_e / q$$

For a point charge

$V=kQ/r$ relative to zero at infinity

Potential difference, $V=kQ (1/r_f - 1/r_i)$

(like gravitational potential, $V=E_g/m$)

For uniform field

$$V=E_e/q = Eqd/q = Ed$$

You can use this to determine the electric field between parallel plates with potential difference, V , a distance d apart.

$$E=V/d$$

Equipotential lines - show where the voltage is constant in space.

Rules-

Always parallel to conductors

Always perpendicular to field lines

The spacing is determined by the electric field

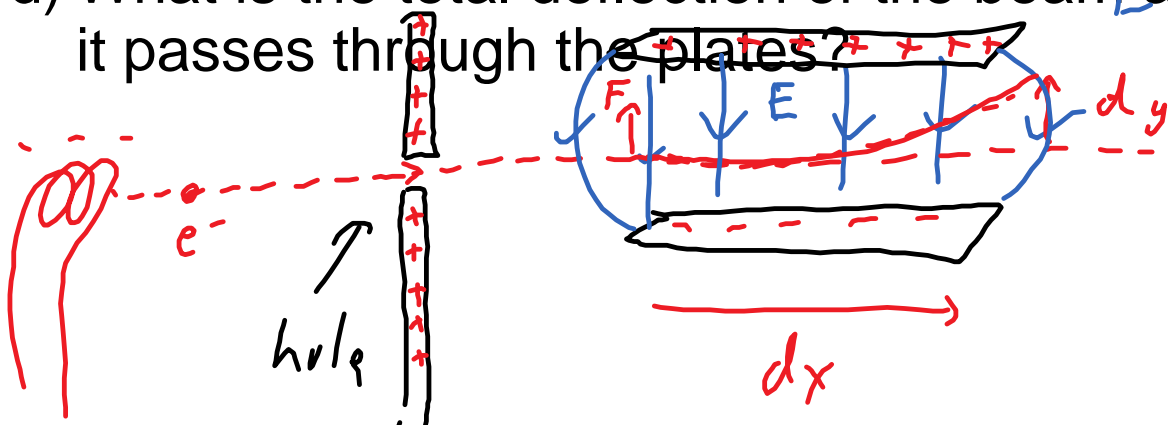
$V=Ed$ for uniform field or kQ/r for point charges

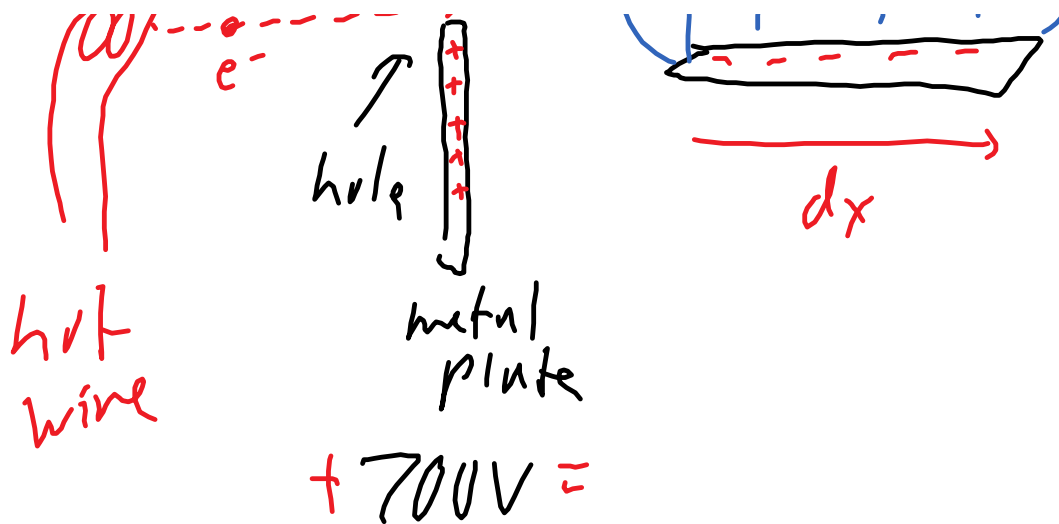
1. A 6.0 micro coulomb charge is 20.0 cm from a -3.5 micro coulomb charge.

- a) What is the force between the charges?
- b) What is the electrostatic energy of the $-3.5\mu\text{C}$ charge relative to zero at infinity?
- c) What is the field strength at the midpoint between the charges?
- d) What is the potential at the midpoint between the charges?
- e) What is the field strength and potential 5.0 cm above the midpoint?
- f) How much work is done moving the $-3.5\mu\text{C}$ charge 5.0 cm closer?
- g) Draw field lines and equipotential lines.

2. A cathode ray tube has an accelerating voltage of 700V before going between two parallel plates, 0.50 cm apart, 4.0 cm long and 20.0V of potential between them.

- a) What is the speed of an electron after being accelerated by 700V?
- b) What is the field strength between the parallel plates?
- c) What is the acceleration of the electron between the plates?
- d) What is the total deflection of the beam as it passes through the plates?

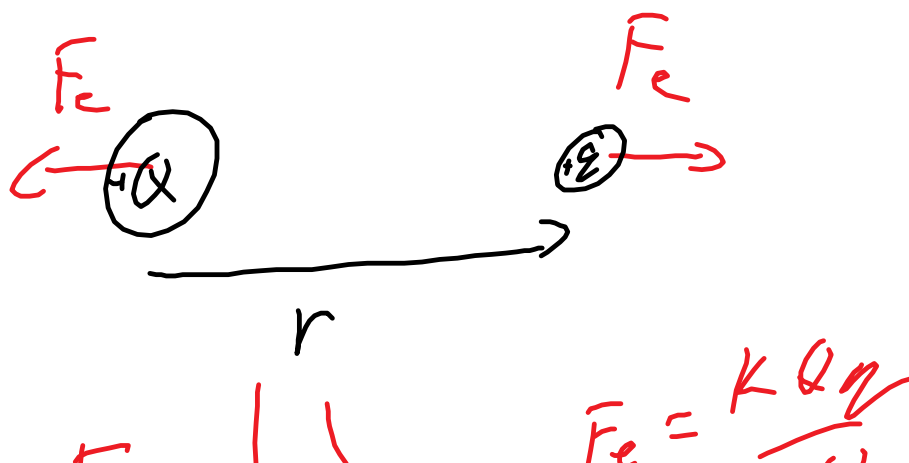


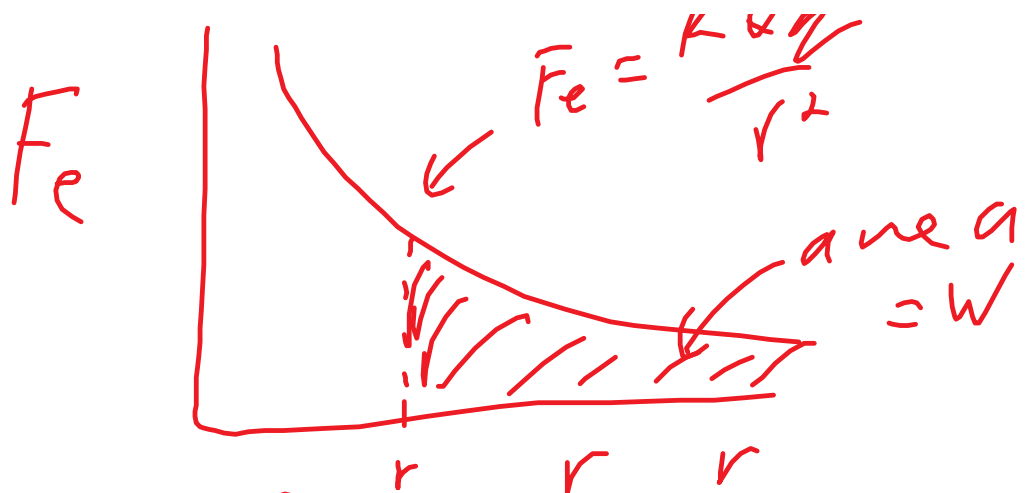


Electrostatic Energy, E_e , and Potential (Voltage) V

Derive expressions for energy using the work-energy theorem.

Work done against the electric field = change in electrical energy





$$\Delta F_e \approx W_e = \int_{\infty}^r F_e dr = \int_{\infty}^r \frac{KQq}{r^2} dr$$

$$F_e = + \frac{KQq}{r}$$

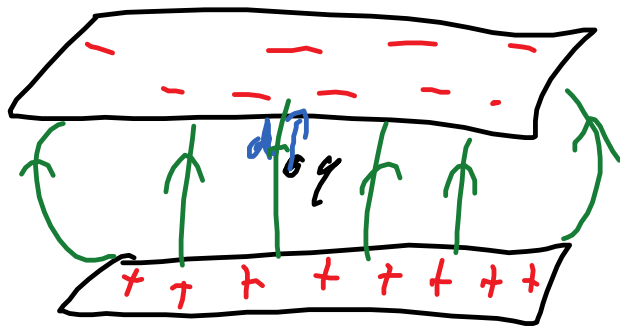
rel to 0 at $r \rightarrow \infty$

Positive because F_e is repulsive
(F_g is attractive)

$$W_e = \Delta F_e = KQq \left(\frac{1}{r_f} - \frac{1}{r_i} \right)$$

In a uniform field, $E = \frac{F}{q}$

- Between parallel plates



$$W = Fd$$

$$W = Eqd$$

Electrostatic Potential = Voltage

$$V = \frac{Ee}{q} \quad \text{Potential difference} = \frac{\Delta Ee}{q}$$

for point charges

$$V = \frac{kQx}{r^2x} = \boxed{\frac{kQ}{r}}$$

for uniform field

$$V = \frac{\Delta Ee}{q} = \frac{Ed}{1} = Ed$$

$$E = \frac{V}{d}$$

field between
two plates, d
apart with potential
 V across.

Equipotential Lines

Show lines of constant electrostatic potential

Rules: don't cross

Perpendicular to field lines

Parallel to conducting surfaces